Spin transport in Magnetic Tunnel Junctions

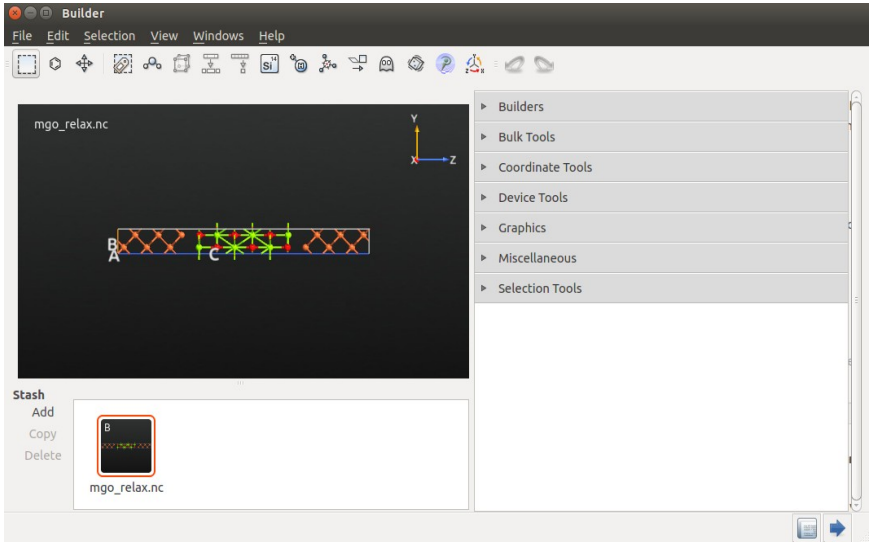
Quantum Wise
When every atom matters

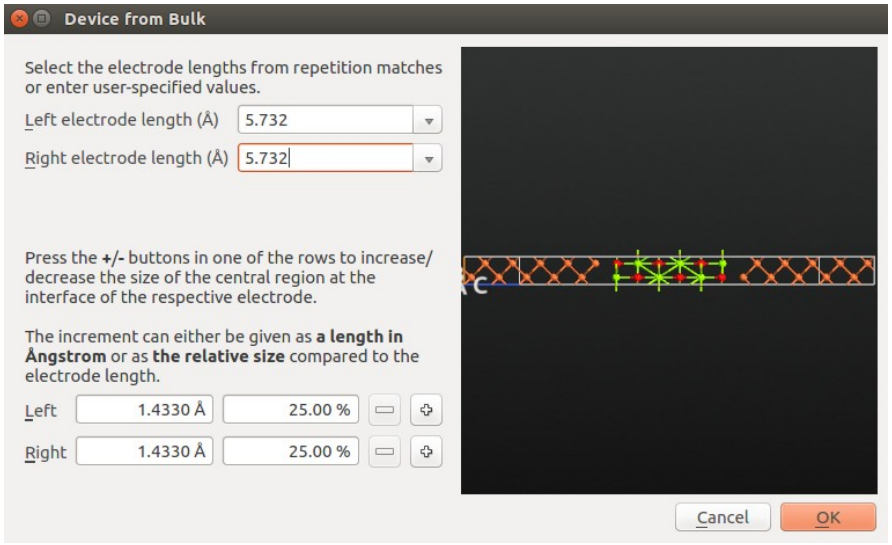
This tutorial shows how to simulate and analyze the electronic transport properties of magnetic tunnel junctions (MTJs). You will study the collinear and non-collinear spin-dependent transport properties of the Fe-MgO-Fe magnetic tunnel junction. In particular you will study the electronic transmission, the tunnel magnetoresistance and the spin-transfer torque.

Setup the MTJ device

Builder

- Download the already relaxed Fe-MgO-Fe geometry and save it in the *Project Folder*.
- Select the bulk configuration and send it to the **Builder**.
- Use **Device Tools → Device From Bulk …** to generate the device structure.
- Send the structure to the **Script Generator**.

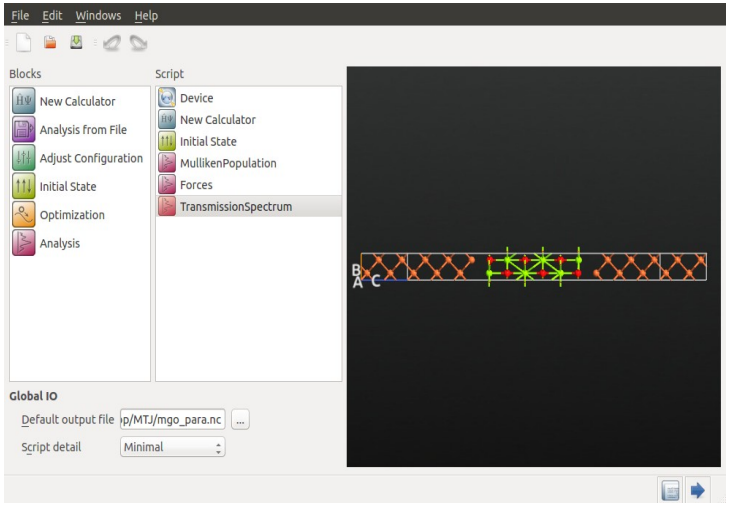


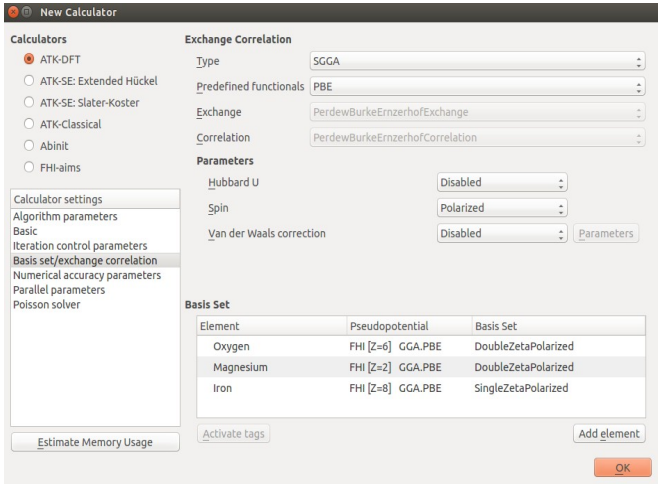


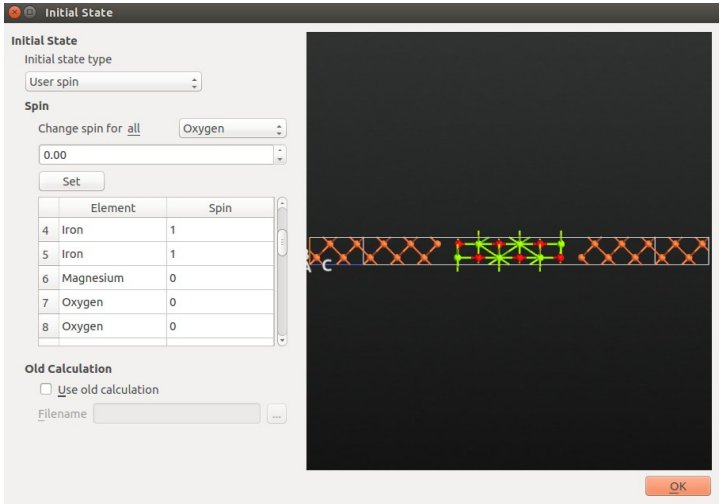
Setup the script for transmission calculation: spin parallel

Script Generator

- New Calculator
  - Spin: Polarized
  - Exchange-correlation: SGGA.PBE
  - Electron temperature: 1200 Kelvin.
  - K-point sampling: (7,7,100)
- Initial State.
  - Initial State: User spin
  - Relative spin: 0 for Mg and O and 1 for Fe.
- MullikenPopulation
- Forces



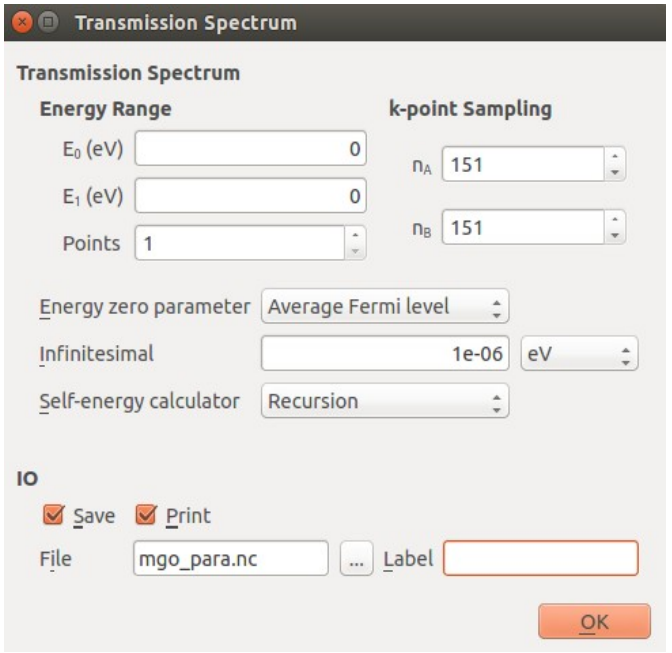




Setup the script for transmission calculation: spin parallel

Script Generator

- TransmissionSpectrum
  - E0=E1= 0 eV
  - Energy Points=1
  - K-points grid sampling: (151x151)



Inspecting the forces

- From the *LabFloor*, select the **Forces** object.
- Next, click **Text Representation...** button.
- The forces on the equivalent electrode atoms inside the central cell are not calculated (zero).
- For the other atoms, the forces are small: relaxing the geometry is a good strategy for this system.

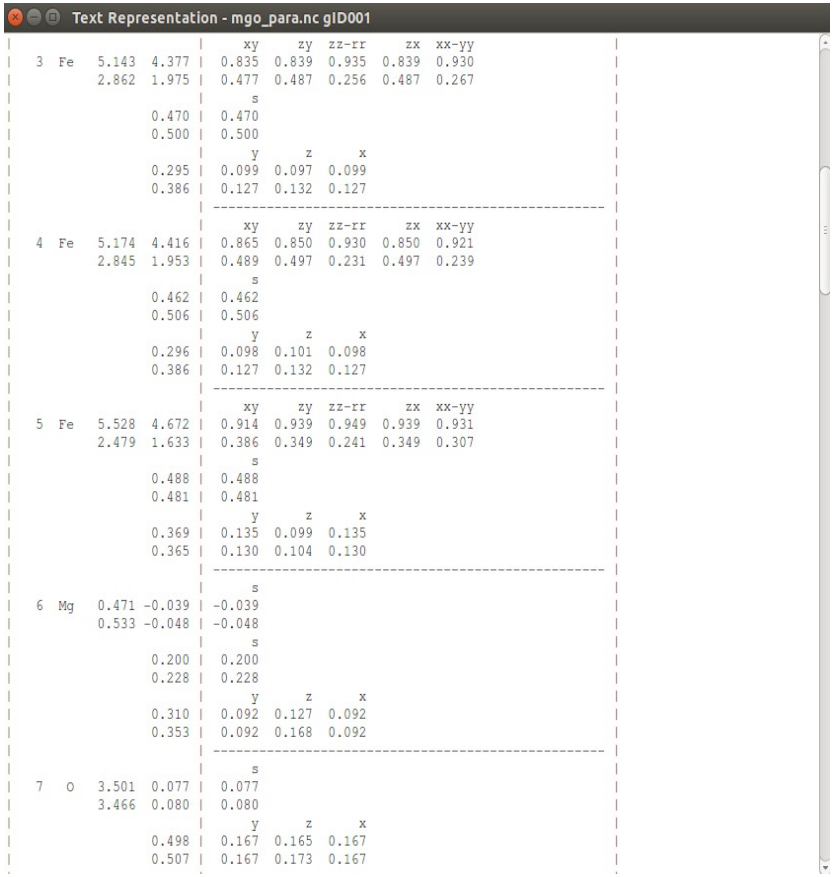
Text Representation - mgo_para.nc gID002

Forces Report

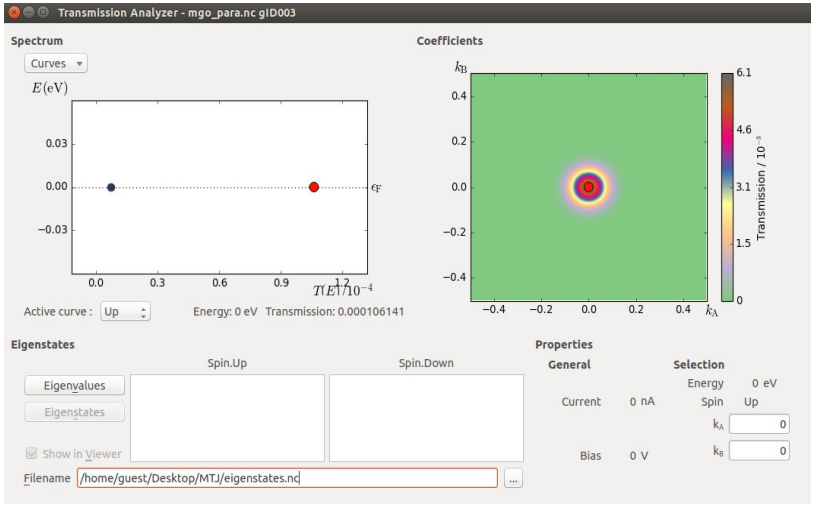
0	[0.	0.	0.] eV/Ang
1	[0.	0.	0.] eV/Ang
2	[0.	0.	0.] eV/Ang
3	[0.	0.	0.] eV/Ang
4	[8.45465615e-12	9.05913388e-12	5.33112605e-02] eV/Ang
5	[6.70492811e-16	3.31813858e-13	5.08472088e-02] eV/Ang
6	[7.53030333e-14	1.35816057e-13	3.06672047e-02] eV/Ang
7	[2.18724856e-13	3.18207716e-13	-4.25977632e-02] eV/Ang
8	[-4.11851333e-13	-2.28127742e-13	3.09332238e-02] eV/Ang
9	[6.88135651e-13	5.54325977e-13	-2.14898256e-02] eV/Ang
10	[1.86181511e-13	2.41570836e-14	2.07259595e-03] eV/Ang
11	[9.79923789e-14	7.76501986e-14	3.44847509e-04] eV/Ang
12	[-1.97227464e-13	-4.04002518e-13	-1.43340421e-03] eV/Ang
13	[3.31820610e-13	4.79069195e-13	-1.64169392e-03] eV/Ang
14	[1.33074350e-13	2.38848958e-13	2.23690384e-02] eV/Ang
15	[1.54185790e-13	2.26209719e-13	-3.13143948e-02] eV/Ang
16	[1.55243033e-14	-1.93859661e-13	4.15923983e-02] eV/Ang
17	[5.24342233e-13	3.84586029e-13	-3.15909400e-02] eV/Ang
18	[4.02378062e-13	2.89209107e-13	-4.55259672e-02] eV/Ang
19	[7.63754107e-12	7.97428998e-12	-4.40655240e-02] eV/Ang
20	[0.	0.	0.] eV/Ang
21	[0.	0.	0.] eV/Ang
22	[0.	0.	0.] eV/Ang
23	[0.	0.	0.] eV/Ang

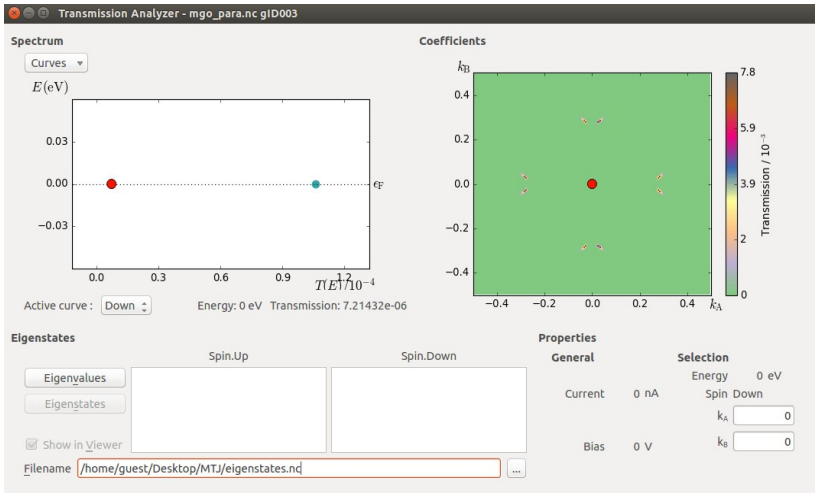
Inspecting the Mulliken Population

- From the *LabFloor*, select the **MullikenPopulation** object.
- Click **Text Representation...** button.
- Check that each atom is correctly spin polarized: Inspect the leftmost column, this shows the total Mulliken population per spin channel for each atom.
- All the Fe atoms polarized with their majority spin pointing up.
- The Mg atoms close to the interface couple antiparallel with Fe.
- The O atoms are unpolarized.



Analyzing the k-parallel transmission



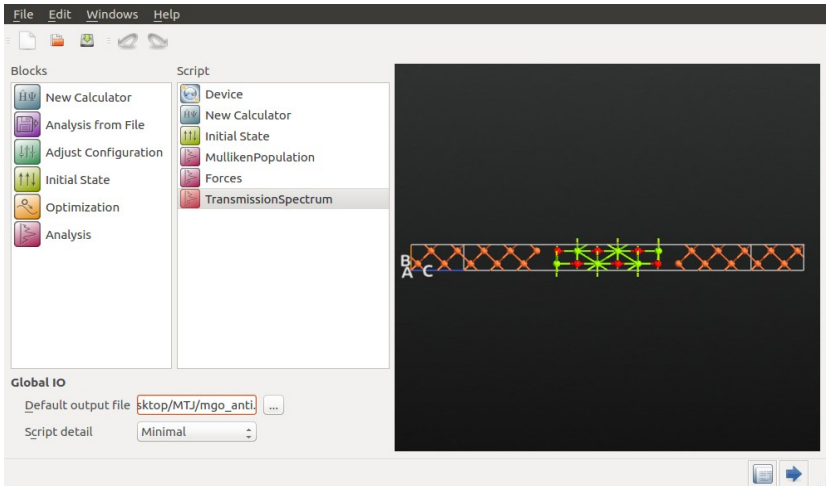


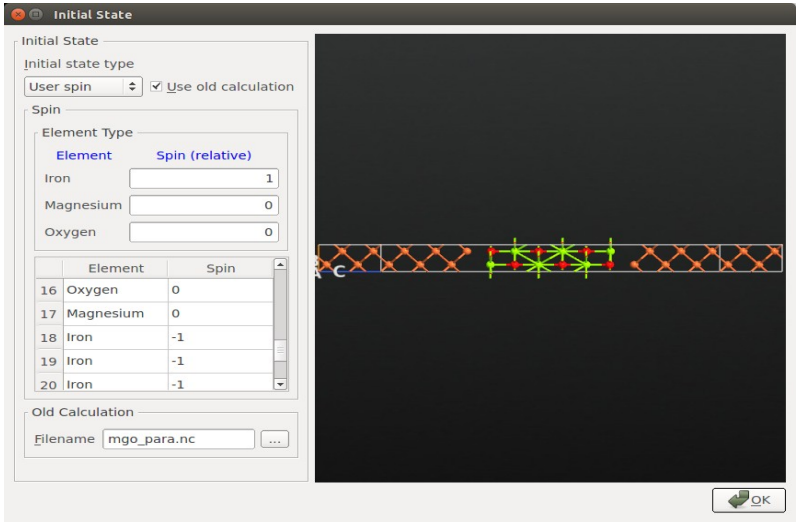
- It is clear from the plots that the down spin (minority) transmission is strongly supressed in magnitude and exhibits peaks at certain points in the Brillouin zone.

Setup the script for Transmission calculation: spin anti-parallel

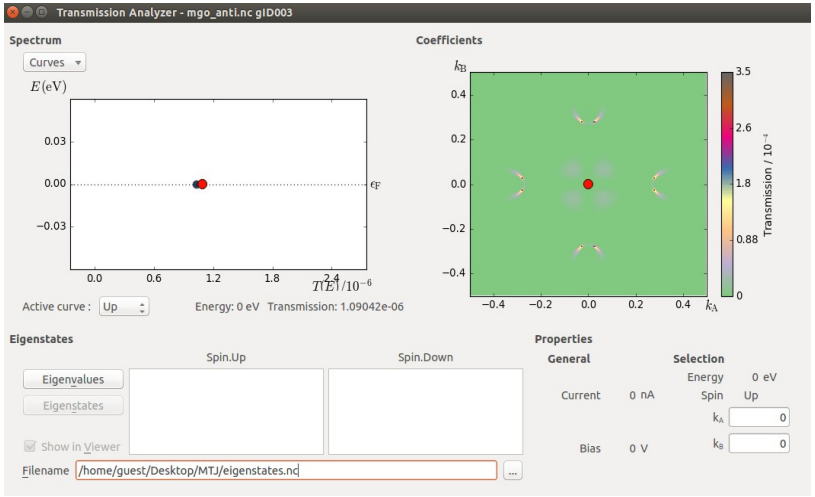
Script Generator

- New Calculator
  - Spin: Polarized
  - Exchange-correlation: SGGA.PBE
  - Electron temperature: 1200 Kelvin.
  - K-point sampling: (7,7,100)
- Initial State.
  - Initial State: User spin
  - Relative spin: 0 for Mg and O and 1/-1 for Fe.
- MullikenPopulation
- Forces
- TransmissionSpectrum
  - E0=E1= 0 eV
  - Energy Points=1
  - K-points grid sampling: (151x151)





Analysis of k anti-parallel transmission



- In this case the transmission for the up and down will be identical due to the mirror symmetry of the system. Note: due to the time inversion symmetry, propagation from left to right is always identical to propagation from right to left.
- The up components of the transmission spectrum corresponds to up electrons from the left transmission propagating into the right electrode.
- The down component of the transmission spectrum corresponds to the down electrons in the right propagating into the left electrode.

Tunneling magnetoresistance

❖ The tunneling magneto resistance (TMR) is defined as:

$$\mathrm{TMR} = \frac{G_P - G_{AP}}{G_{AP}},$$

G_P is the conductance through the junction with parallel spin alignment
G_{AP} is the conductance for the anti-parallel spin alignment

❖ Script provided (**tmr.py**) to calculate the conductance from the transmission spectra of the junction with parallel and anti-parallel spin aligment:

```
# Calculate conductance for parallel spin
transmission_para = nlread('mgo_para.nc', TransmissionSpectrum)[0]
conductance_para_uu = transmission_para.conductance(spin=Spin.Up)
conductance_para_dd = transmission_para.conductance(spin=Spin.Down)
conductance_para = conductance_para_uu + conductance_para_dd

# Calculate conductance for anti-parallel spin
transmission_anti = nlread('mgo_anti.nc', TransmissionSpectrum)[0]
conductance_anti_uu = transmission_anti.conductance(spin=Spin.Up)
conductance_anti_dd = transmission_anti.conductance(spin=Spin.Down)
conductance_anti = conductance_anti_uu + conductance_anti_dd

print 'Conductance Parallel Spin (Siemens)'
print 'Up=%8.2e, Down=%8.2e' % (conductance_para_uu.inUnitsOf(Siemens),
                                conductance_para_dd.inUnitsOf(Siemens))
print 'Total = %8.2e' % (conductance_para.inUnitsOf(Siemens))
print

print 'Conductance Anti-Parallel Spin (Siemens)'
print 'Up=%8.2e, Down=%8.2e' % (conductance_anti_uu.inUnitsOf(Siemens),
                                conductance_anti_dd.inUnitsOf(Siemens))
print 'Total = %8.2e' % (conductance_anti.inUnitsOf(Siemens))
print

print 'TMR (optimistic)  = %8.2f percent' % \
      (100.*(conductance_para-conductance_anti)/conductance_anti)
print 'TMR (pessimistic) = %8.2f percent' % \
      (100.*(conductance_para-conductance_anti)/(conductance_para+conductance_anti))
```

❖ Execute the script and find the TMR:

```
Conductance Parallel Spin (Siemens)
Up=4.11e-09, Down=2.79e-10
Total = 4.39e-09

Conductance Anti-Parallel Spin (Siemens)
Up=4.22e-11, Down=4.00e-11
Total = 8.22e-11

TMR (optimistic)  =  5240.12 percent
TMR (pessimistic) =    96.32 percent
```

Adaptive k-grid

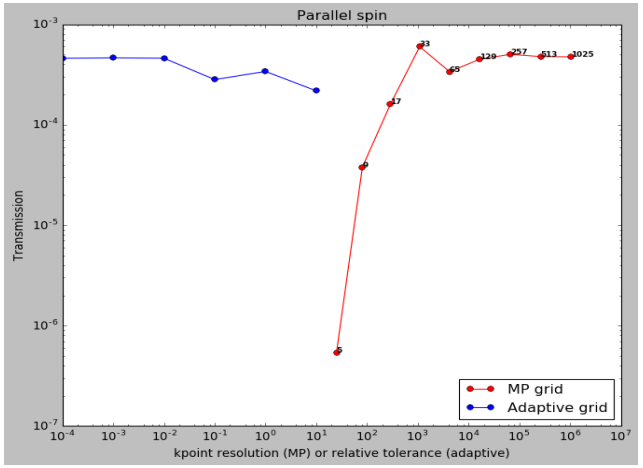
- Object for defining the k-point sampling used for the calculation of transmission and spin-transfer torque.
- **Application**: automatically zoom in on the significant features of the electron transmission spectrum. Useful when the k-dependent transmission is dominated by localized peaks and the total computed transmission may depend critically on resolving those peaks.
- **Adaptive algorithm**: divides the Brillouin zone into triangles and integrates over each triangle. Each triangle becomes increasingly small in an iterative manner until convergence is reaced, but stops if the number of refinement levels reaches the **max_number_of_levels** (20 by default).
- The integral over each triangle is estimated as:
- In order to estimate whether or not the I_o integral is converged, two types of errors available:
  - Absolute: converged when the absolute value of the Brillouin zone integral in all triangles is lower than the chosen tolerance
  - Relative: converged when the relative value of the Brillouin zone integral in all triangles is lower than the chosen tolerance.

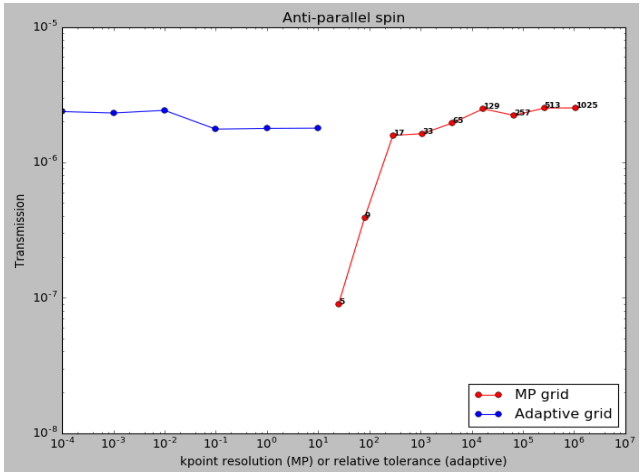
- Absolute or Relative error? If one have knowledge about the function values, the use of Absolute error may be advantageous, otherwise the use of Relative error will be more useful.

Adaptive grid vs. MonkhorstPack grid: total transmission convergence at 0 eV

Transmission computed for Parallel and antiparallel configurations

- Basis set: *DoubleZetaPolarized* for Mg and O. *SingleZetaPolarized* for Fe.
- Exchange and correlation: SGGA.PBE
- K-point sampling: 6,6,100
- Electron temperature: 1200 Kelvin
- Adaptive k-grid
  - Relative Tolerance: 10, 1, 0.1, 0.01, 0.001, 0.0001 and 0.00001.
- Monkhorst-Pack grid
  - K-pont sampling: (5x5), (9x9), (17x17), (33x33), (65x65), (129x129), (257x257), (513x513), (1025x1025)





Well converged calculations of the total transmission through the MTJ obtained with no less than 10^3 Monkhorst-Pack k-points and with a relative tolerance of 10^{-2} using the adaptive k-point grid.

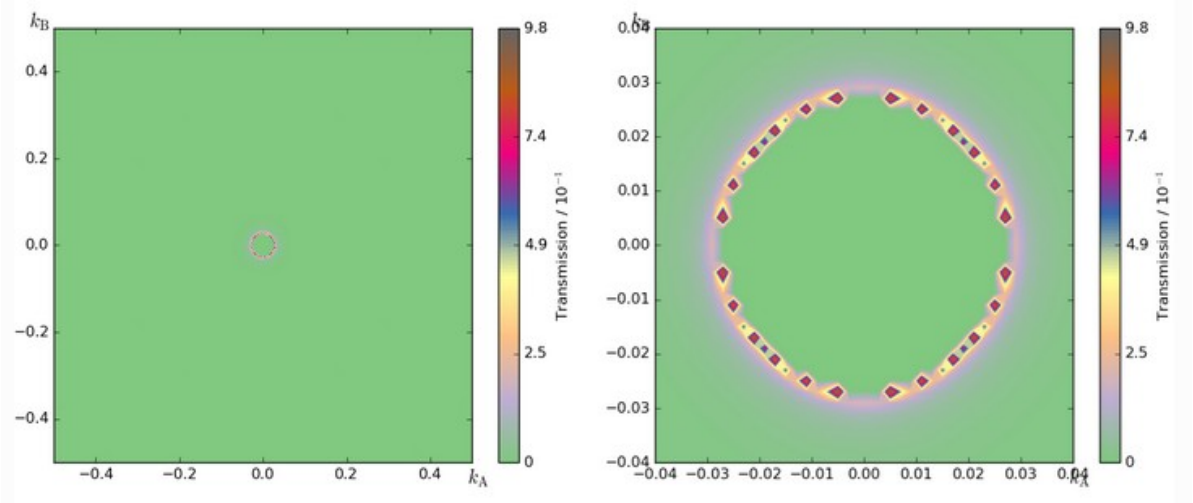
Parallel transmission

- Provide the adaptive_grid.py script.
- This script calculates the transmission for the Fe|MgO|Fe device with parallel spin orientation using both a dense MP grid and the AdaptiveGrid method.
- Monkhorst-Pack grid: 500x500 k-points
- Adaptive grid: relative tolerance of 10^{-2}.
- Download and run the script.

```
# ----------------------------------------------------------------------
# Load device configuration
# ----------------------------------------------------------------------
device_configuration = nlread('mgo_para.nc', DeviceConfiguration)[0]

# ----------------------------------------------------------------------
# Transmission Spectrum using a dense Monkhorst-Pack grid.
# ----------------------------------------------------------------------
transmission_spectrum = TransmissionSpectrum(
    configuration=device_configuration,
    energies=numpy.linspace(0,0,1)*eV,
    kpoints=MonkhorstPackGrid(500,500),
    )
nlsave('adaptive_grid.nc', transmission_spectrum)

# ----------------------------------------------------------------------
# AdaptiveGrid.
# ----------------------------------------------------------------------
adaptive_grid = AdaptiveGrid(
    tolerance=0.01,
    error_measure=Relative)

# ----------------------------------------------------------------------
# Transmission Spectrum using the AdaptiveGrid.
# ----------------------------------------------------------------------
transmission_spectrum = TransmissionSpectrum(
    configuration=device_configuration,
    energies=numpy.linspace(0,0,1)*eV,
    kpoints=adaptive_grid,
    )
nlsave('adaptive_grid.nc', transmission_spectrum)
```

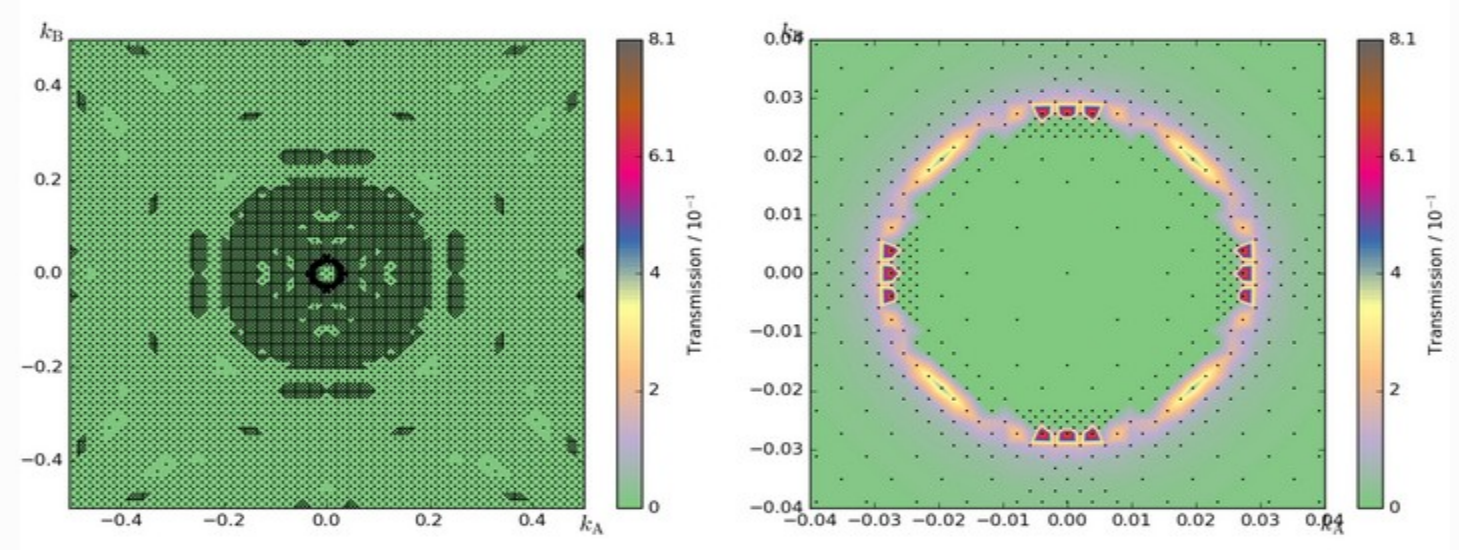
Spin-up transmission – Monkhorst-Pack grid

- Transmission spectrum obtained using a MP grid of (500x500) k-point sampling.



- The transmission spectrum obtained with the dense MP grid is different from the one obtained before using (151x151) k-point sampling.
  - Now circular feature in the middle of the spectrum with zero transmission immediately around the gamma point.
  - The improved k-point sampling has only increased the total k-point averaged spin-up transmission by a factor of 4.

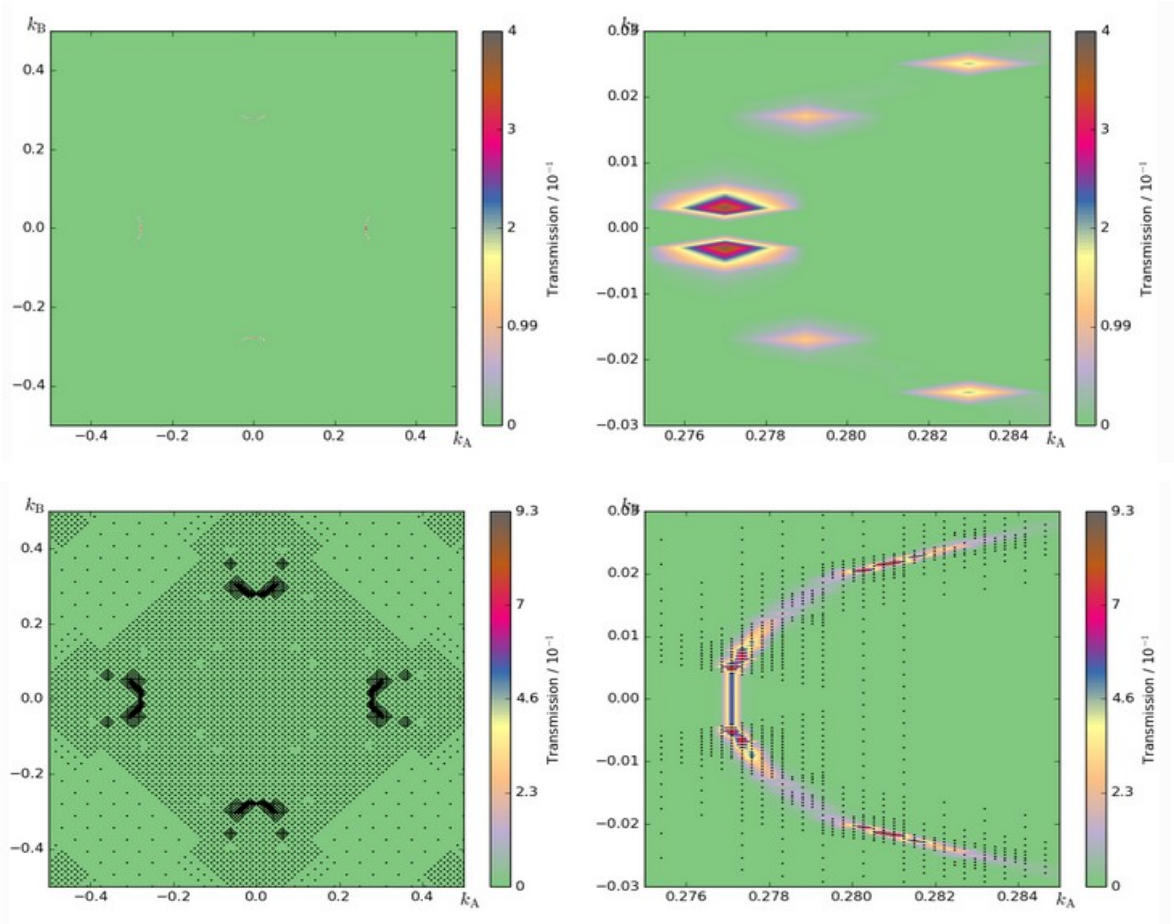
Spin-up transmission – Adaptive grid



- Spin-up transmission spectrum evaluated using the Adaptive grid with a 10^{-2} relative tolerance.
- Black dots indicate the sampled k-points.
- The adaptive grid has zoomed in on the circular feature of the k-dependent transmission, causing a larger k-point density around the circular feature.

Spin-down transmission

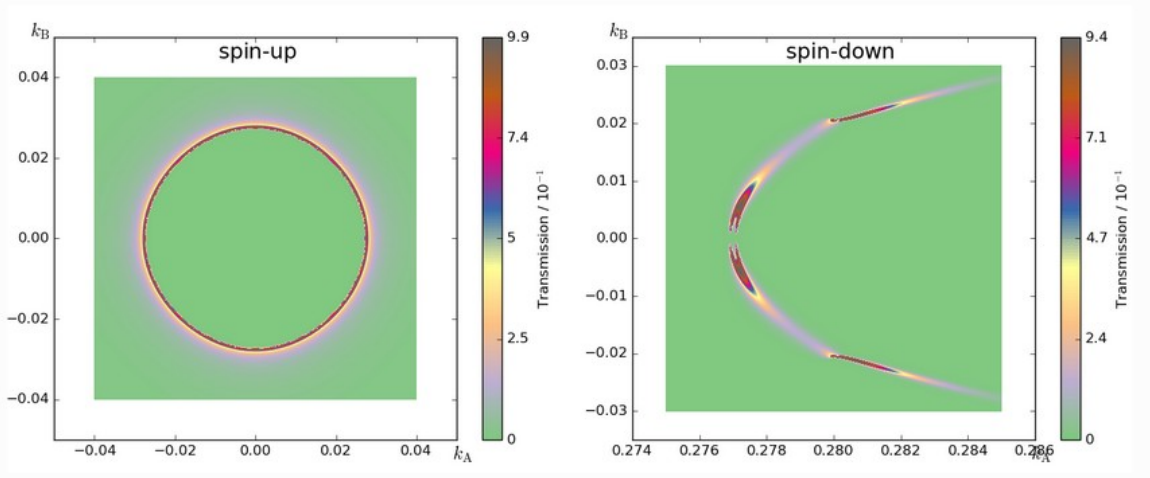
- Above, transmission obtained using Monkhorst-Pack grid. The total k-point averaged spin-down transmission is 3.7 10^{-5}.
- Below, transmission obtained using Adaptive grid. The total k-point averaged spin-down transmission is 3.5 10^{-5}.
- The adaptive grid has zoomed in on the transmission peaks.
- The total k-point averaged spin-down transmission has changed 5%.



Restricting the grid range

- Provide the zoom.py script.
- This script shows how the adaptive grid class can be used to resolve only a specific features of the spin-up and spin-down k-dependent transmission.
- A relative tolerance of 10^{-3} is used to fully resolve the transmission features.
- The below figures show the spin-up and spin-down transmissions.

```
# ----------------------------------------------------------------------
# Load device configuration
# ----------------------------------------------------------------------
device_configuration = nlread('mgo_para.nc', DeviceConfiguration)[0]

# ----------------------------------------------------------------------
# Transmission Spectrum zoom #1.
# ----------------------------------------------------------------------
adaptive_grid = AdaptiveGrid(
    kA_range=[-0.04, 0.04],
    kB_range=[-0.04, 0.04],
    tolerance=0.001,
    error_measure=Relative)

transmission_spectrum = TransmissionSpectrum(
    configuration=device_configuration,
    energies=numpy.linspace(0,0,1)*eV,
    kpoints=adaptive_grid,
    )
nlsave('zoom.nc', transmission_spectrum)

# ----------------------------------------------------------------------
# Transmission Spectrum zoom #2.
# ----------------------------------------------------------------------
adaptive_grid = AdaptiveGrid(
    kA_range=[0.275, 0.285],
    kB_range=[-0.03, 0.03],
    tolerance=0.001,
    error_measure=Relative)

transmission_spectrum = TransmissionSpectrum(
    configuration=device_configuration,
    energies=numpy.linspace(0,0,1)*eV,
    kpoints=adaptive_grid,
    )
nlsave('zoom.nc', transmission_spectrum)
```



Computing the non-collinear device configuration

Editor

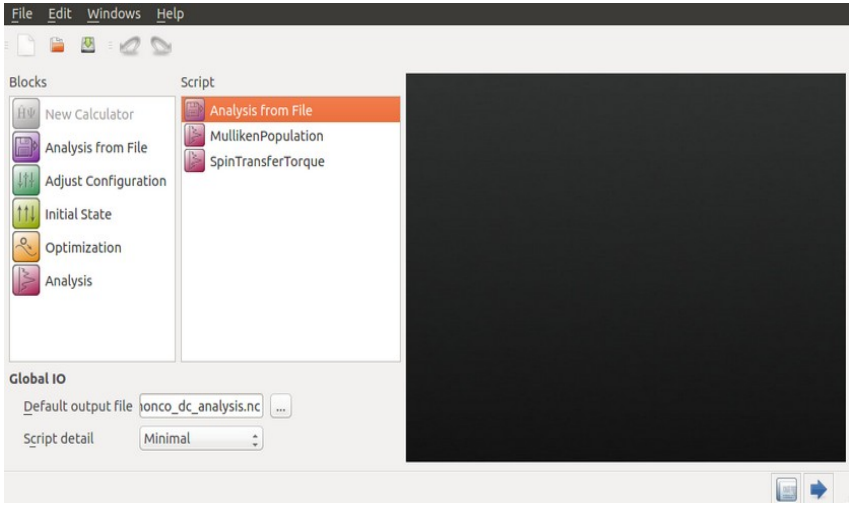
- Requires non-collinear definition of the electron spin.
- Device configuration: read the collinear configuration mgo_para.nc
- New Calculator : replace SGGA.PBE by NCGGA.PBE exchange and correlation.
- Define the spin rotation: theta= 120 degrees
- Setup the initial state: new calculator and spin
- Update and save the device configuration.

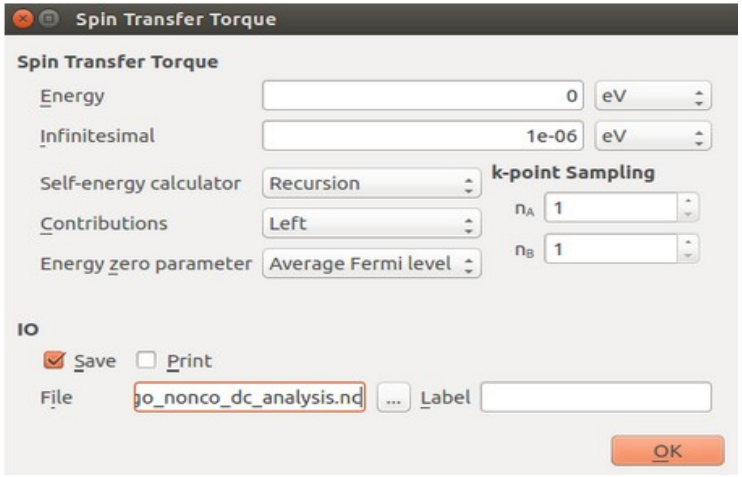
```
# Read in the collinear calculation
device_configuration = nlread('mgo_para.nc', DeviceConfiguration)[0]

# Use the special noncollinear mixing scheme
iteration_control_parameters = IterationControlParameters(
    algorithm=PulayMixer(noncollinear_mixing=True)
    )
# Get the calculator
calculator = device_configuration.calculator()
new_calculator = calculator(
       exchange_correlation=NCGGA.PBE,
       iteration_control_parameters = iteration_control_parameters
       )
# Define the spin rotation
theta = 120*Degrees
left_spins = [(i, 1, 0*Degrees, 0*Degrees) for i in range(3)]
center_spins = [(i+3, 1, theta*i/5, 0*Degrees) for i in range(6)]
right_spins = [(i+9, 1, theta, 0*Degrees) for i in range(3)]
spin_list = left_spins+center_spins+right_spins
initial_spin = InitialSpin(scaled_spins=spin_list)

# Setup the initial state
device_configuration.setCalculator(
    calculator=new_calculator,
    initial_spin=initial_spin,
    initial_state=device_configuration)

# Calculate and save
device_configuration.update()
nlsave("mgo_nonco_dc.nc", device_configuration)
```

Mulliken population and Spin Transfer Torque

Scripter

- Analysis from file
  - Select the mgo_nonco_dc.nc file
- MullikenPopulation
- SpinTransferTorque.
  - Energy: 0eV
  - Contributions: Left to calculate **left → right** linear response current.
  - Send the script to the Editor and replace the Monkhorst-Pack grid by the Adaptive grid.

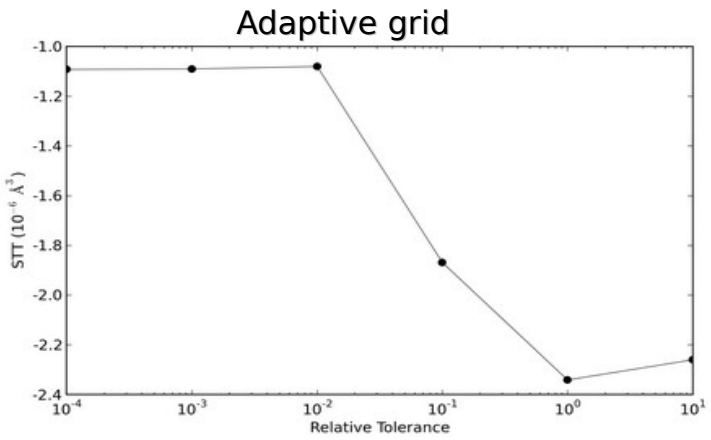


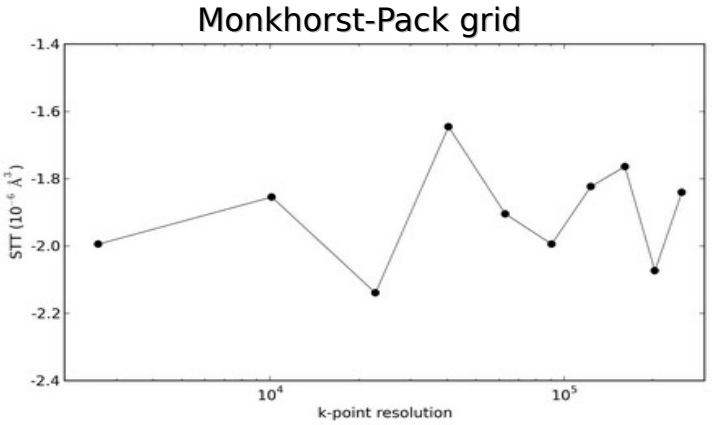



```
# Setup adaptive grid object.
adaptive_grid = AdaptiveGrid(
        kA_range=[-0.5, 0.5],
        kB_range=[-0.5, 0.5],
        tolerance=1e-2,
        error_measure=Relative,
        )
# ------------------------------------------------------------------
# Spin Transfer Torque
# ------------------------------------------------------------------
spin_transfer_torque = SpinTransferTorque(
    configuration=device_configuration,
    energy=0*eV,
    kpoints=adaptive_grid,
    contributions=Left,
    energy_zero_parameter=AverageFermiLevel,
    infinitesimal=1e-06*eV,
    self_energy_calculator=RecursionSelfEnergy(),
    )
nlsave('mgo_nonco_dc_analysis.nc', spin_transfer_torque)
```

Convergence of the total spin-transfer torque

- We are using a **relative tolerance of 10^{-2}** for the adaptive grid.
- The spin-transfer torque must be computed using the relative tolerance at which the total transferred torque at the right side is converged.
- We have calculated the total spin-transfer torque in the right side for different relative tolerances.
- Use of 10-2 relative tolerance seems to be sufficient.
- Using a Monkhorst-Pack grid the total spin-transfer torque does not reach the convergence.





Analysis of the results

Mulliken Population

- Inspect the Mulliken charge and the components of the spin polarization vector using the text representation.
- The sum of up and down populations corresponds to the Mulliken charge (number of electrons) .
- The difference of these populations combined with the two angles (Theta and Phi) forms the spin polarization vector. This vector can be visualized using the Viewer.

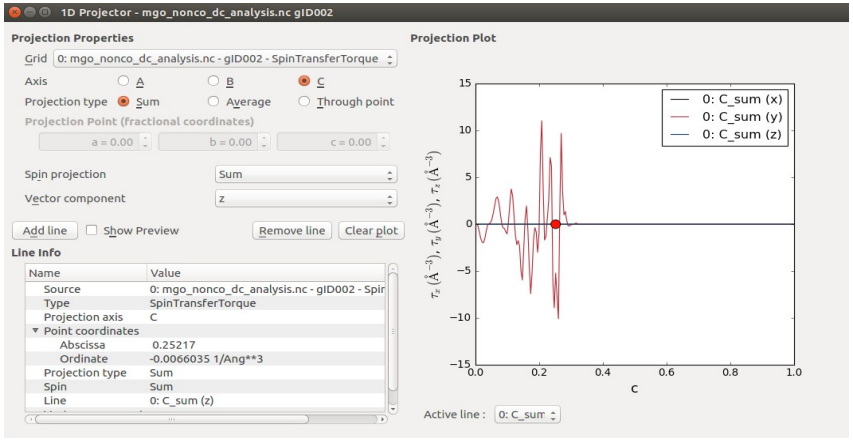
Text Representation - mgo_nonco_dc_analysis.nc gID001

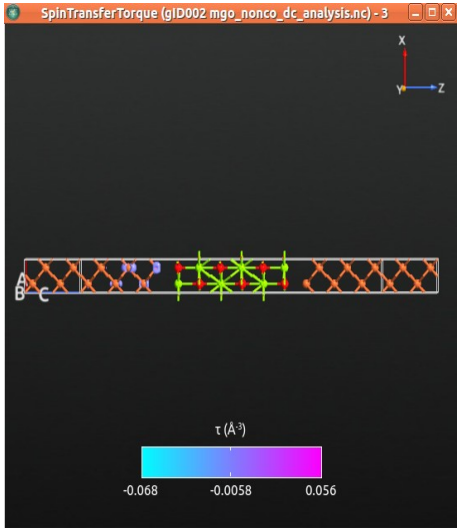
Element	Up	Down	Theta (Degrees)	Phi (Degrees)
0 Fe	5.0867	2.9217	0.0677	359.7676
1 Fe	5.0633	2.9370	0.1560	180.1813
2 Fe	5.0576	2.9400	0.0348	358.7518
3 Fe	5.1583	2.8468	0.5838	180.1091
4 Fe	5.1849	2.8335	24.8154	0.0034
5 Fe	5.5418	2.4686	49.8978	359.9971
6 Mg	0.5278	0.4751	135.7503	180.0182
7 O	3.4988	3.4673	65.4680	0.0035
8 O	3.5211	3.5194	59.5990	0.0220
9 Mg	0.4820	0.4752	37.2865	359.6952
10 Mg	0.4789	0.4786	52.7842	1.2203
11 O	3.5218	3.5216	30.5324	0.2408
12 O	3.5218	3.5216	2.1668	0.0697
13 Mg	0.4788	0.4787	11.8829	358.7890
14 Mg	0.4819	0.4753	0.0557	0.7770
15 O	3.5210	3.5195	0.0599	359.8667
16 O	3.5008	3.4657	0.0004	359.9098
17 Mg	0.5326	0.4722	179.9986	0.1708
18 Fe	5.5300	2.4769	0.0000	179.5913
19 Fe	5.1796	2.8391	0.0000	359.9876
20 Fe	5.1499	2.8555	0.0000	180.0096
21 Fe	5.0520	2.9460	0.0000	0.0127
22 Fe	5.0695	2.9308	0.0000	359.6984
23 Fe	5.0823	2.9116	0.0000	0.0180

Analysis of the results

Spin-transfer torque

- The spatial components of the spin-transfer torque can be plotted using the **1D Projector**.
- Visualize the spatial components of the Spin-transfer torque using the Viewer. The below figure shows the isosurface of the “y” component.



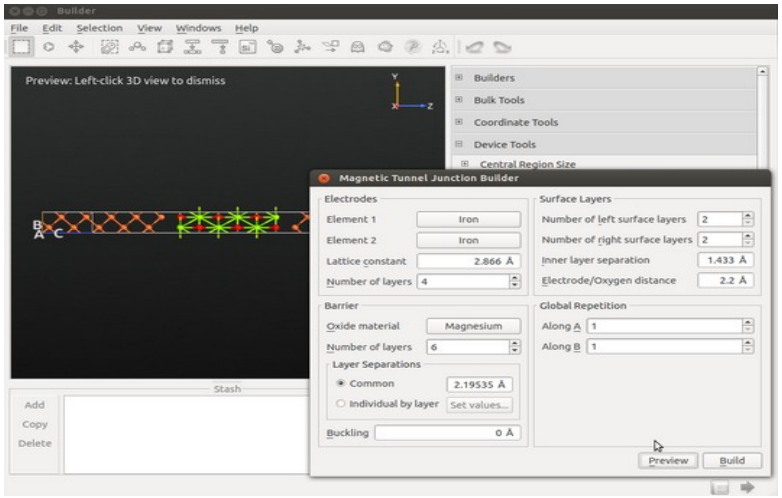


Optimizing the junction geometry

Builder

1.- Use Add → From Plugin → Magnetic Tunnel Junction (FeMgO-style). Change the number the barriers to 6 and number to surface layers to 2 on both left and right side and leave the other parameters as they are by default.

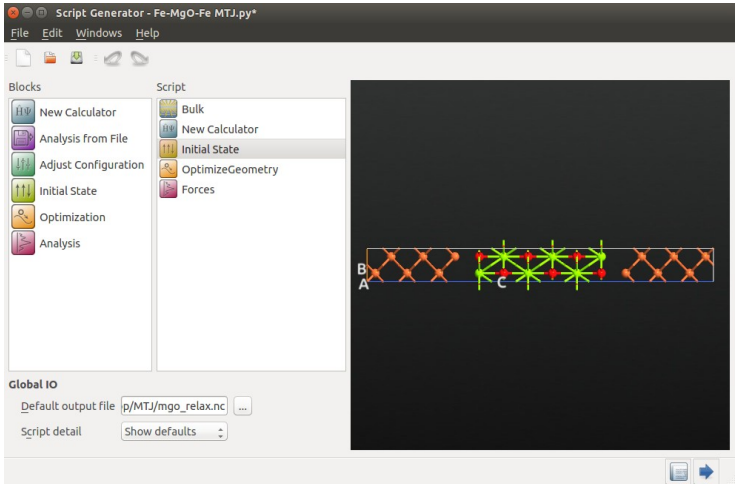
2.- Convert the device geometry to bulk send the structure to the Script Generator to optimize it by keeping **Rigid** the last two layers of Fe.

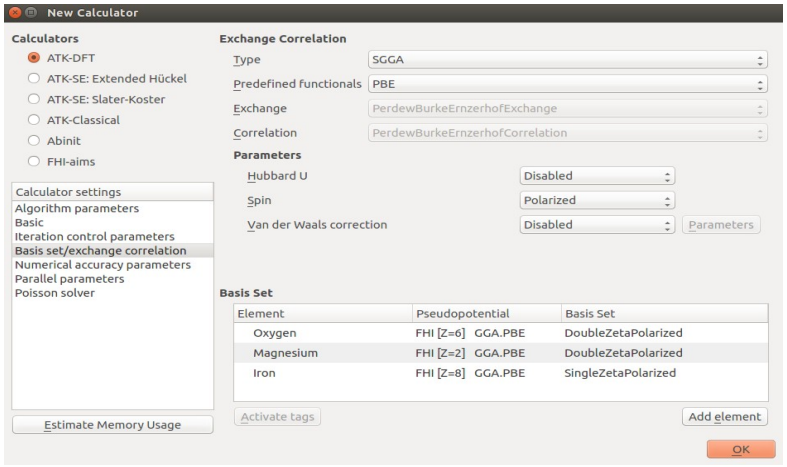


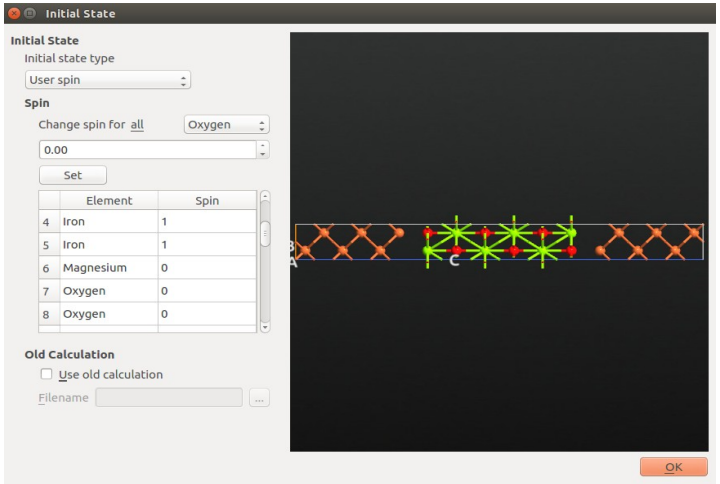
Optimizing the junction geometry

Script Generator

- New Calculator
  - Spin: Polarized
  - Exchange-correlation: SGGA.PBE
  - Electron temperature: 1200 Kelvin.
  - K-point sampling: (7,7,100)
- Initial State.
  - Initial State: User spin
  - Relative spin: 0 for Mg and O and 1 for Fe.



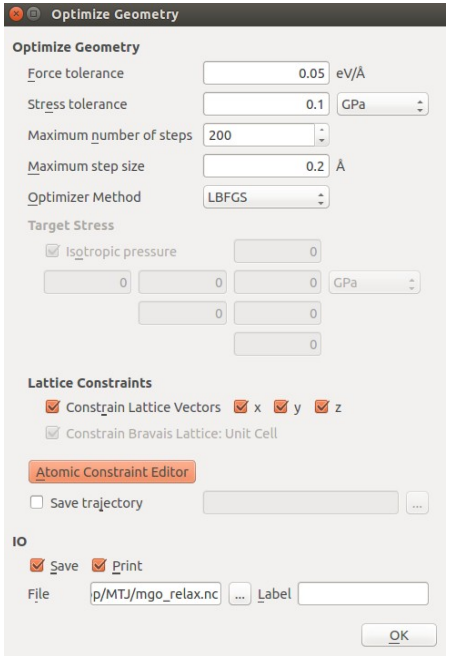


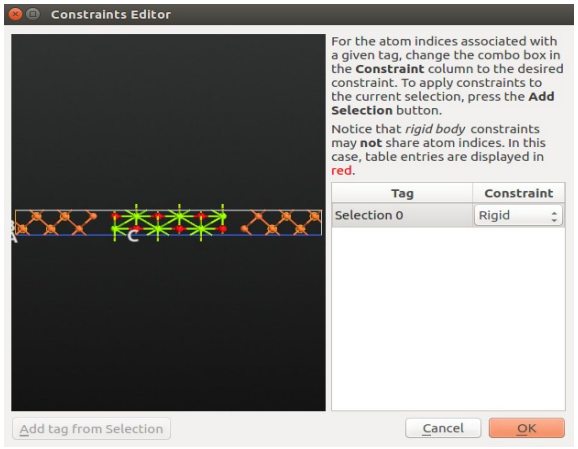


Optimizing the junction geometry

Script Generator

- OptimizeGeometry
  - Keep the first and last four atoms rigid.
- Forces





Analysis of the results

Forces

- Zero in x-y direction.
- Less that the optimization criteria (0.05 eV/Ang) for atoms which have been relaxed.
- For the electrode extension the forces are slightly larger and the force vectors point out of the cell (cell under compressive strain).
- Adding more surface to increase the cell length in z direction would lower the strain but would have very little effect on the results in the present case.

Text Representation - mgo_relax.nc gID002

```
# Item:  0
# File:  /home/guest/Desktop/MTJ/mgo_relax.nc
# Title: mgo_relax.nc - gID002
# Type:  Forces
+-------------------------------------------------------------------------------+
| Forces Report                                                                 |
+-------------------------------------------------------------------------------+
|   0  [ -5.65166433e-13  -2.98611144e-13  -9.01817935e-02] eV/Ang               |
|   1  [  6.64493502e-12   6.52651480e-12   2.94255336e-02] eV/Ang               |
|   2  [  1.36823030e-12   1.95106286e-12  -1.00136659e-01] eV/Ang               |
|   3  [ -8.80667107e-12  -8.91005512e-12  -1.28493796e-01] eV/Ang               |
|   4  [  6.51485018e-12   6.03326508e-12   4.26430559e-02] eV/Ang               |
|   5  [  2.04540092e-12   1.95944348e-12   4.62198920e-02] eV/Ang               |
|   6  [ -2.37574737e-13   1.70103226e-13   2.44565333e-02] eV/Ang               |
|   7  [  5.65371777e-13   4.78715809e-13  -1.87839167e-02] eV/Ang               |
|   8  [  6.44396562e-13   3.09377807e-14   4.22671554e-02] eV/Ang               |
|   9  [ -3.17920036e-13   1.90817595e-13  -1.78024014e-02] eV/Ang               |
|  10  [  2.39036696e-13  -1.42687211e-13   6.38323635e-03] eV/Ang               |
|  11  [ -9.01442166e-14   3.67834264e-13   5.32441803e-03] eV/Ang               |
|  12  [  4.81927740e-13   6.67437624e-14  -6.05958779e-03] eV/Ang               |
|  13  [  8.34988325e-14   1.70593147e-13  -5.67429277e-03] eV/Ang               |
|  14  [ -2.10890956e-14   3.37287204e-14   1.85028336e-02] eV/Ang               |
|  15  [  4.25436429e-13   7.27451603e-14  -4.28807194e-02] eV/Ang               |
|  16  [  1.86917685e-13   1.50087159e-13   1.85504931e-02] eV/Ang               |
|  17  [  6.00559901e-13   2.32819142e-13  -2.46488340e-02] eV/Ang               |
|  18  [  1.37458279e-12   1.99913731e-12  -4.16245073e-02] eV/Ang               |
|  19  [  4.42454411e-12   5.54030364e-12  -3.40699334e-02] eV/Ang               |
|  20  [ -5.65094164e-12  -7.22871690e-12   1.17937925e-01] eV/Ang               |
|  21  [  8.76830526e-12   1.10265548e-11   9.98868244e-02] eV/Ang               |
|  22  [ -1.87565300e-11  -2.07851072e-11  -3.01908210e-02] eV/Ang               |
|  23  [ -7.04845969e-14  -2.85051189e-13   9.13089459e-02] eV/Ang               |
+-------------------------------------------------------------------------------+
```